Third Semester B.E. Degree Examination, Dec.09/Jan.10 Engineering Mathematics - III

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

1 a. Obtain Fourier series for the function f(x) given by

$$f(x) = \begin{cases} 1 + \frac{2x}{\pi}, & -\pi \le x \le 0 \\ 1 - \frac{2x}{\pi}, & 0 \le x \le \pi \end{cases}$$

and hence deduce that $\frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$

(07 Marks)

b. Find the half-range cosine series for the function $f(x) = (x-1)^2$ in the interval 0 < x < 1.

(07 Marks)

Obtain the constant term and the coefficients of the first sine and cosine terms in the Fourier expansion of y as given in the following table. (06 Marks)

 x
 0
 1
 2
 3
 4
 5
 6

 y
 9
 18
 24
 28
 26
 20
 9

2 a. Find the Fourier transform of $f(x) = \begin{cases} 1 - x^2, & |x| \le 0 \\ 0, & |x| > \pi \end{cases}$

Hence evaluate $\int_{0}^{\infty} \frac{x \cos x - \sin x}{x^{3}} \cdot \cos \left(\frac{x}{2}\right) dx$

(07 Marks)

b. Find the Fourier cosine transform of e-x2

(07 Marks)

c. Find the Fourier sine transform of $e^{-|x|}$. Hence show that $\int_{0}^{\infty} \frac{x \sin mx}{1+x^2} dx = \frac{\pi}{2} e^{-m}, m > 0.$

(06 Marks)

3 a. Form the partial differential equation by eliminating the arbitrary functions f and g from the relation $z = y^2 + 2f\left(\frac{1}{x} + \log y\right)$ (07 Marks)

b. Solve
$$\frac{\partial^3 t}{\partial x^2 \partial y} + 18xy^2 + \sin(2x - y) = 0$$
 (07 Marks)

c. Solve
$$(mz - ny)\frac{\partial z}{\partial x} + (nx - lz)\frac{\partial z}{\partial y} = (ly - mx)$$
 (06 Marks)

4 a. Derive one dimensional heat equation by taking u(x, t) as the temperature, x is the distance and t is the time. (Write the figure also.)

(07 Marks)

b. Obtain the D'Almbert's solution of the wave equation $u_{tt} = C^2 u_{xx}$, subject to the condition u(x, o) = f(x) and $\frac{\partial u}{\partial t}(x, o) = o$. (07 Marks)

c. Obtain the various solutions of the Laplace's equation $u_{xx} + u_{yy} = 0$, by the method of separation of variables. (06 Marks)

PART - B

- 5 a. Complete the real root of the equation $x\log_{10}x 1.2 = 0$ by Regula-Falsi method, correct to four decimal places. (07 Marks)
 - b. Solve the system of equations using Gauss-Jordan method:

$$2x + 5y + 7z = 52$$

 $2x + y - z = 0$
 $x + y + z = 9$ (07 Marks)

c. Using the power method, find the largest Eigen value and the corresponding Eigen vector of

the matrix
$$A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$$
 (06 Marks)

6 a. The area of a circle (A) corresponding to diameter (D) is given below:

(07 Marks)

D	80	85	90	95	100
A	5026	5674	6362	7088	7854

Find the area corresponding to diameter 105 using an appropriate interpolation formula.

b. Use Newton's divided difference formula to find f(9), given the data,

(07 Marks)

X	5	7	11	13	17
f(x)	150	392	1452	2366	5202

c. Evaluate $\int_{4}^{5.2} \log_{e} x \, dx$ using Weddle's rule, taking 7 ordinates.

(06 Marks)

7 a. Derive Euler's equation in the form

$$\frac{\partial f}{\partial y} - \frac{d}{dx} \left(\frac{\partial f}{\partial y'} \right) = 0 \tag{07 Marks}$$

- b. Find the curves on which the functional $\int_{0}^{1} [(y')^{2} + 12xy] dx$, with y(0) = 0 and y(1) = 1 can be extremised. (07 Marks)
- c. Find the geodesics on a surface given that the arc length on the surface is $S = \int_{x_1}^{x_2} \sqrt{x[1+(y')]} dx$ (06 Marks)
- 8 a. Find the Z-transforms of the following:

i)
$$\cosh n\theta$$
 ii) $(n+1)^2$

(07 Marks)

- b. Find the inverse z-transform of $\frac{z}{(z-1)(z-2)}$. (07 Marks)
- c. Find the response of the system $y_{n+2} 5y_{n+1} + 6y_n = u$, with $y_0 = 0$, $y_1 = 1$ and $u_n = 1$ for $n = 0, 1, 2, 3, \dots$ by z-transform method. (06 Marks)

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Third Semester B.E. Degree Examination, Dec.09/Jan.10

Electronic Circuits

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

 a. With a neat diagram and waveforms, explain the working of a positive camper with respect to the stiff clamper condition. (08 Marks)

b. An LED is used in the indicator circuit for the a.c. power line of 230V AC with 50Hz frequency. The circuit consists of a capacitor of 0.68μf. Calculate the capacitive reactance and average LED current.

e. Explain with relevant diagrams, the principle of operation of a varactor diode. (08 Marks)

Explain with a neat circuit diagram and a.c. equivalent circuit, the working of base biased amplifier.

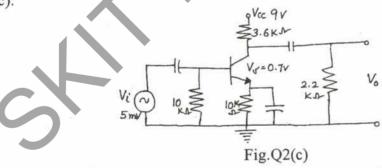
(08 Marks)

b. Sketch the output waveform for the clipper circuit of Fig. 2(b) shown below. Assume silicon diode and obtain the peak magnitude of the output waveform.



Fig. (2(b) (06 Marks)

c. Find the voltage gain and output voltage across the load resistor for the given circuit of FigQ2(c).



(06 Marks)

a. Explain the working of a swamped amplifier with a neat circuit diagram. Derive the expression for voltage gain.

(08 Marks)

b. Draw the cascaded CE and CC stages of amplifier. Explain. (06 Marks)

c. Derive an expression for an output voltage for a series feedback type regulator. (06 Marks)

4 a. Explain the principal of operation of class B push-pull amplifier with a neat circuit diagram and relevant waveforms.

(08 Marks)

b. In a class B amplifier, $V_{CE(min)} = 1$ volt, supply voltage $V_{CC} = 18$ volts. Calculate the collector circuit efficiency. (04 Marks)

 c. What is digital switching? Explain in detail passive load switching and active load switching.
 (08 Marks)

- What is impedance matching? Explain. (04 Marks) Explain briefly decibel power gain and decibel voltage gain. (06 Marks)
 - c. Explain ideal closed loop voltage gain, gain stability, closed loop input impedance, closed loop output impedence and non linear distortion, with respect to VCVS amplifier. (10 Marks)
- With relevant details, explain VCIS amplifier.

(06 Marks)

b. Write a note on comparators with nonzero references.

(06 Marks)

- c. With a neat circuit diagram and waveforms, explain the sine wave to rectangular converter, using OP-AMP. (08 Marks)
- a. Explain the principle of relaxation oscillator to generate rectangular output. Draw a neat circuit diagram and waveform. (08 Marks)

b. Explain with a neat connection diagram and waveforms, how IC555 timer is used as a stable multivibrator. (08 Marks)

What do you know about phase locked loops? Explain.

(04 Marks)

- 8 Write an explanatory note on:
 - Opto electronic devices
 - b. Load lines in power amplifier
 - Voltage controlled oscillator
 - Switching regulators.

(20 Marks)

Third Semester B.E. Degree Examination, Dec.09/Jan.10 Logic Design

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, choosing at least two from each part.

PART-A

- 1 a. Implement AB+C D with only three NAND gates. Draw logic diagram also. Assume inverted input is available. (06 Marks)
 - b. Reduce the following functions using K-map techniques.

i) $f(P,Q,R,S) = \Sigma m (0, 1, 4, 8, 9, 10) + d(2, 11)$

ii) $f(A,B,C,D) = \Pi m (0, 2, 4, 10, 11, 14, 15).$

(06 Marks)

c. Reduce the following function by using quine McClusky method $f(A, B, C, D) = \sum m (0, 1, 2, 3, 10, 11, 12, 13, 14, 15)$.

(08 Marks)

2 a. Define an encoder. Design a priority encoder the truth table of which is shown in table Q2(a). The order of priority of inputs is $X_1 > X_2 > X_3$

Inputs				Outputs	
S	X ₁	X2	X ₃	A	В
0	X	х	X	0	0
1	1	х	X	0	- 1
1	0	1	X	1	0
1	0	0	1	-1	1
1	0	0	0	0	0

Table Q2(a)

(06 Marks)

- b. What is magnitude comparator? Write the truth table and circuit diagram of a 1 bit comparator. (06 Marks)
- c. Mention different types of ROMS and explain each of them.

(08 Marks)

- 3 a. Show the 8-bit addition of following decimal numbers into 2's compliment representation i) +125 and -68 ii) +37 and -115 iii) -43 and -78. (06 Marks)
 - b. What is a full adder? Give the truth table of full adder. From this truth table design a full adder circuit. (08 Marks)
 - c. Explain the working of a parallel adder. What are its advantages and disadvantages over a serial adder? (06 Marks)
- 4 a. What is a system clock? What are the characteristics of an ideal clock?

(06 Marks)

b. Show how a D flip-flop can be converted to SR flip-flop.

- (06 Marks)
- Explain the working of a JK flip-flop. Write its truth table, state diagram and excitation table.

PART-B

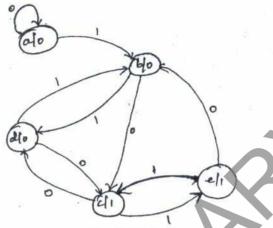
- 5 a. Name and explain in short the four basic types of shift registers and draw a block diagram for each. (06 Marks)
 - b. Mention the differences between ripple and synchronous counters. (06 Marks)
 - Design a synchronous mod-3 counter with the following binary sequence using clocked JK flip-flops.

Counter sequence 0, 1, 2, 0, 1, 2.

(08 Marks)

- a. Write a note on Moore and Mealy models with respect to design of sequential circuits.
 Compare the two models. (06 Marks)
 - b. Draw an ASM chart for a 2-bit counter having one enable line E such that E = 1 (counting enabled) E = 0 (counting disabled). (06 Marks)
 - c. Reduce state transition diagram (Moor model) of Fig. Q6(c) by
 - i) Row elimination method
 - ii) Implication table method.

(08 Marks)



- Fig. Q 6(c)
- 7 a. What is the binary ladder? Explain the binary ladder with a digital input of 1000. (06 Marks)
 - b. What is accuracy and resolution of the D/A converter. What is the resolution of a 9-bit D/A converter which uses a ladder network? If the full scale output voltage of this converter is + 5V, what is the resolution in volts? (06 Marks)
 - c. Explain continuous A/D conversion with an example.

(08 Marks)

8 a. What is a MOSFET? Explain its working

- (06 Marks)
- b. Discuss the features of high speed TTL, low power TTL, Schottky TTL families. (06 Marks)
- c. Explain method for interfacing CMOS devices to TTL devises.

(08 Marks)

USN

Third Semester B.E. Degree Examination, Dec.09/Jan.10

Discrete Mathematical Structures

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART-A

a. Let x be the set of all three digit integers that is $x = \{x \text{ is an integer } / 100 \le x \le 999\}$. If A_i is the set of numbers in x whose ith digit is i, compute the cardinality of the set $A_1 \cup A_2 \cup A_3$. (05 Marks)

b. Using the laws of set theory, simplify each of the following:

i) $A \cap (B-A)$

ii) $(A \cup B) \cap C \cup B$

(05 Marks)

c. State and prove Demorgan's laws set theory.

(05 Marks)

d. Among the integers 1-200 find the numbers of integer's that are:

Divisible by 2 or 5 or 9

ii) Not divisible by 5

iii) Not divisible by 2 or 5 or 9

iv) Divisible by 5 or not by 2 or 9

(05 Marks)

a. Define tautology S.T 2

 $[(pvq) \cap (p \to r) \land (q \to r)] \to r$ is a tautology by constructing truth table.

(05 Marks)

b. Prove the following by using laws of logic

(05 Marks)

i) $p \to (q \to r) \Leftrightarrow (p \land q) \to r$ ii) $[\sim p \land (\sim q \land r)] \lor [(q \land r) \lor (p \land r)] \Leftrightarrow r$ c. Verify the principles of duality for the logical equivalence :

 $i) \ \ \sim (p \wedge q) \rightarrow \sim pv(\sim p \vee q) \Leftrightarrow \sim p \vee q \qquad ii) \ P.T. \big[p \wedge (p \rightarrow q) \wedge r \big] \Rightarrow (p \vee q) \rightarrow r \qquad (05 \ Marks)$

d. Check whether the following is a valid argument:

If I study, then I will not fail in the examination. If I do not watch T.V. in the evening I will study.

failed in the examination

(05 Marks)

I must have watch T.V. in the evening.

Define an open statement. Write down the negation of following statements:

For all integer 'n' if n is not divisible by 2 then n is odd.

If k, m, n are any integers when (k - m) and (m - n) are odd then (k - n) is even.

(05 Marks)

For the universe of all integers, define the following open statements:

Let p(x): x > 0, s(x): x is divisible by 3, q(x): x is even, r(x): x is a perfect square, t(x): xis divisible by 7. Write down the following quantified statements in symbolise form:

At least one integer is even

ii) Some even integers are divisible by 3

iii) For every integer is either even or odd

iv) If x is even and a perfect square then x is not divisible by 3

(05 Marks)

If x is odd or is not divisible by 7 then x is divisible by 3. $PT \exists x q(x)$ follows logically from the premises $\forall x p(x) \rightarrow q(x)$ and $\exists x p(x)$ c. i)

ii) PT the following argument is valid where 'C' is the specification element of universe $\forall x [p(x) \rightarrow q(x)]$

$$\forall x [q(x) \rightarrow r(x)]$$

v)

(05 Marks)

(05 Marks)

 $\sim r(c)/:..\sim p(c)$

d. Give direct proof of the statement if n is odd integer and n² is an odd integer.

(05 Marks)

(05 Marks)

(05 Marks)

(05 Marks)

(05 Marks)

mathematical induction that for integer $1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$ (05 Marks) b. A sequence $\{a_n\}$ is defined successively by $a_1 = 4$, $a_n = a_{n-1} + n$, for $n \ge 2$ find an explicit form. c. The fibonacci numbers are defined recursively by $F_0=0$, $F_1=1$ and $F_n=F_{n-1}+F_{n-2}$ for $n\geq 2$. Evaluate F_2 to F_{10} . (05 Marks) d. The Ackermann's number. $A_{m,n}$ are defined recursively for $m, n \in \mathbb{N}$ as follows: $A_{o,n} = n + 1$, for $n \ge 0$ $A_{m,o} = A_{m-1,1}$ for $m \ge 0$ $A_{m,n} = A_{m-1,p}$ where $p = A_{m,n-1}$ form $m, n \ge 0$ P.T. $A_{1,n} = n + 2$ for all $n \in \mathbb{N}$ (05 Marks PART – B a. Let $A = \{1 \ 2 \ 3 \ 4\}$. Let 'R' be a relation on A defined by xRy iff x/y and y = 2x write down: 5 i) 'R' is a relation of set of ordered pairs ii) Draw di-graph of R iii) Determine in degrees and out-degrees of a diagraph (05 Marks) b. Define the following terms and give an example for each: i) Reflexive ii) Irreflexive iii) Anti symmetric iv) Transitive v) Symmetry (05 Marks) c. Let R be an equivalence relation on A and (ab) \(\) then ST the following statement are: i) $a \in [a] \text{ or } a \in R(a)$ ii) aRb iff, [a] = [b] or R(a) = R(b)iii) $[a] \cap [b] \neq \emptyset$ then [a] = [b](05 Marks) d. Draw the hasse diagram respresented by the positive divisor of 36. (05 Marks) a. Let $A = B = \{1 \ 2 \ 3 \ 4\}$ i) $f = (1 \ 1) (2 \ 3) (3 \ 4) (4 \ 2)$ (ii) let $A = \{a \ b \ c\}, B = \{1 \ 2 \ 3 \ 4\} f = \{(a \ 1) \ (b \ 1) \ (c \ 4)\}$ iii) $A = \{1 \ 2 \ 3 \ 4\}, b = \{a \ b \ c \ d\}, f = \{(1 \ a) \ (2 \ a) \ (3 \ d) \ (4 \ c)\}.$ Determine 'f' is one-one of on to. (05 Marks) b. If m and n are positive integers with $1 \le n \le m$, P.T. $s(m+1, n) = s(m, n-1) + n \cdot s(m, n)$ (05 Marks) c. If $f: A \rightarrow B$ is invertible then it has unique inverse. d. State Pigeon-hole principle If (n + 1) number are chosen from 1 to 2n at least one pair add to (2n + 1)(05 Marks) Define Abelian group. Prove that a group G is abelian if and only if for all a, b ∈ G, 7 (05 Marks) b. Define a cyclic group show that every cyclic group is abelian but the converse is not true. (05 Marks) c. State and prove Lagrange's theorem. (05 Marks) d. Let $f: G \to H$ be a homomorphism from G into H. If G is abelian, prove that H is also

2 of 2

ii) For all $a \in S$, we have $-a \in S$

abelian.

a. Prove that every field is an integral domain.

i) For all a, $b \in S$, we have $a + b \in S$ and $ab \in S$

d. Prove that Zn is a field if and only if n is a prime.

b. S is a subring of R if and only if:

c. Show that Z_5 is an integral domain.

Third Semester B.E. Degree Examination, Dec.09/Jan.10 Data Structures with 'C'

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

a. Given the following declarations: 1

int a = 5:

int b = 7;

int *p = & a;

int *q = & b;

What is the value of each of the following expressions?

- i)
- ii) ++(*p)
- iii) --(*q)
- - b iv)

(04 Marks)

- Explain the following with an example:
 - Pointer to pointer i)
 - L value and R value ii)
 - Calloc function.

(09 Marks)

Write a 'C' program to find the smallest element in an array (using pointer and function).

(07 Marks)

Explain with syntax strncpy and streat string handling functions.

(06 Marks)

- Write short notes on:
 - Nested structures i)
 - Union. ii)

(08 Marks)

Explain the three file status functions available in 'C' language.

(06 Marks)

What is a stack? Indicate how stack is represented in 'C'. 3 a.

(05 Marks)

Write an algorithm to evaluate postfix expression. b.

(06 Marks)

- c. Convert each of the following infix expressions into its postfix and prefix form
 - (A + B) * C D E * Fi)
 - A-B/C*D\$E ii)
 - (A + B) * (C + D E) * F.

(09 Marks)

Write a recursive program to find the greatest common divisor (GCD) of two integers.

(06 Marks)

- b. Explain:
 - Efficiency of recursion i)
 - Priority queue. ii)

(06 Marks)

c. Write a C program to simulate the working of linear queue. Provide the following operations: i) insert ; ii) delete ; iii) display. (08 Marks)

PART - B

- 5 a. What are the advantages and disadvantages of representing a stack or queue by a linked list?
 (04 Marks)
 - b. Write a C program to implement stack operations using singly linked list.

(10 Marks)

c. Write a note on noninteger and nonhomogeneous list.

(06 Marks)

6 a. Explain with figure circular list with a header node.

(05 Marks)

- b. Write a C routine concat (& list 1, & list 2) that concatenates two circular singly linked lists.
 (05 Marks)
- c. Assume that first and last are external pointers to the first and last nodes of a doubly linked list. Write an algorithm to implement the following:
 - i) Insert a node to the list at the front end.
 - ii) Delete a node from the front end

(10 Marks)

- 7 a. Define the following (write appropriate figures)
 - i) Strictly binary tree
 - ii) Complete binary tree
 - iii) Almost complete binary tree.

(09 Marks)

- b. What is a binary search tree? Construct a binary search tree for the following list of integers. 8, 13, 10, 12, 6, 5, 12.
- c. Write a C routine setleft (NODEPTR P, int x) which creates a node with information x, as left son of a node pointed by P, in a right in threaded binary tree. (05 Marks)
- 8 a. Write an algorithm to find the Kth element of a list represented by binary tree. Explain the algorithm also. (05 Marks)
 - b. Construct a binary tree for the following expressions:
 - i) A + (B C) * (E + F) / G
 - ii) (5+6*7)\$ ((5+6)*7).

(10 Marks)

c. Convert the following general tree shown in Fig. 8 c(i) and 8 c(ii) to a binary tree (05 Marks)

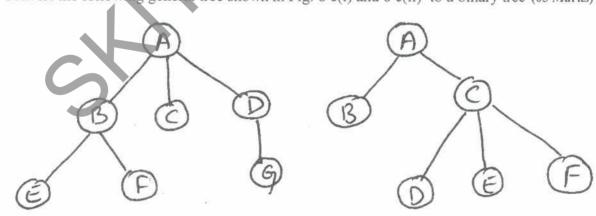


Fig. 8 c(i).

Fig.8 c(ii).

2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice. Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

Third Semester B.E. Degree Examination, Dec.09/Jan.10 Unix and Shell Programming

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

		PART – A	
1	a.	Define an operating system. Discuss the salient features of UNIX operating system.	
1.70	a.	(06 Marks)	
	b.	Explain the architecture of the UNIX operating system. (08 Marks)	
	c.	Explain the following commands with examples: i) cat; ii) rmdir; iii) pwd. (06 Marks)	
2	a.	A file's current permission are rw_r_xr Specify the chmod expression required to change them for the following:	
		i) rw x rw x rw x; ii) rr; iii); iv)r_r (08 Marks)	
		Using both the relative and absolute methods of assigning permissions.	
	b.	Explain briefly the file attributes listed using ls – l command. (06 Marks)	
		What are the different modes of Vi editor? Explain with a diagram. (06 Marks)	
3	a.	Explain what wild – card patterns match:	
		i) [A-Z]???** ii) * [0-9] *	
		iii) $*[!0-9]$ and iv) $*\cdot[!s][!h]$. (08 Marks)	
	b.	What are standard input, standard output and standard error? Explain with respect to UNIX.	
		(06 Marks)	
	c.	What is process status? Explain PS command with options. (06 Marks)	
4	a,	Explain the following environment variables with examples:	
		i) SHELL ; ii) LOGNAME ; iii) PATH. (06 Marks)	
	b.	Differentiate between hard link and soft link in UNIX with examples. (06 Marks)	
	c.	Explain the following commands with examples: i) tail; ii) paste; iii) tr; iv) pr. (08 Marks)	
		PART - B	
5	a.	What is the difference between a wildcard and a regular expression? Explain the "grep" command using n. Land f options with examples. (08 Marks)	
	L.	Communication and any	
		What do these regular expressions match? i) $a \cdot *b$; ii) 6 \$. (04 Marks) What is sed? With examples explain the difference between line addressing and context	
	c.	addressing in sed? (08 Marks)	
6		What is shell programming? Write a shell program that will do the following tasks, in order:	
U	a.	Clear the screen	
		Print the current directory	
		Display current login users. (08 Marks)	
	b.	Explain the shell features of "while" and "for" with syntax. (08 Marks)	
	c.	What is the "exit" status of a command and where is it stored? (04 Marks)	
7	a.	Write an awk program to find square of all the numbers from 1 to 10. (08 Marks)	
	b.		
		i) FS; ii) NF; iii) FILENAME. (06 Marks)	
	c.	Explain the following built-in functions of awk with examples:	
		i) substr; ii) index; iii) length. (06 Marks)	
8	a.	Explain the following string handling functions of PERL with examples:	
		i) length; ii) index; iii) substr; iv) reverse. (08 Marks)	
	b.	Write a PERL program to print numbers that are accepted from the keyboard using while	
		and an array construct. (06 Marks)	
	c.	Explain the following in PERL with examples:	
		i) Foreach looping construct; ii) Join. (06 Marks)	

Third Semester BE Degree Examination, Dec.09-Jan.10 Advanced Mathematics – I

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions.

1 a. Find the modulus and amplitude of $\frac{4+2i}{2-3i}$. (06 Marks)

b. Express the complex number $2 + 3i + \frac{1}{1-i}$ in the form of a + ib. (07 Marks)

c. Express the complex number $\sqrt{3} + i$ in the polar form. (07 Marks)

2 a. Find the nth derivative of e^{-x} sin²x. (06 Marks)

b. Find the nth derivative of $\frac{x}{(x-1)(2x+3)} + e^{2x}$. (07 Marks)

c. If $y = \sin^{-1}x$ then prove that $(1 + x^2) y_{n+2} - (2n + 1) xy_{n+1} - n^2y_n = 0$. (07 Marks)

3 a. Using Maclaurin's series expand tanx upto the term containing x³. (06 Marks)

b. Find the angle between the radius vector and tangent to the curve $r = \sin\theta + \cos\theta$. (07 Marks)

c. With usual notations prove that

i) $P = r \sin \phi$

ii)
$$\frac{1}{p^2} = \frac{1}{p^2} + \frac{1}{p^4} \left(\frac{d\mathbf{r}}{d\theta} \right). \tag{07 Marks}$$

4 a. If u = f(r, s, t) where $t = \frac{x}{y}$, $s = \frac{y}{z}$, $t = \frac{z}{x}$ then prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 0$. (06 Marks)

b. If u = f(x + ay) + g(x - ay) then show that $\frac{\partial^2 u}{\partial y^2} = a^2 \frac{\partial^2 u}{\partial x^2}$. (07 Marks)

c. If
$$u = x^2 - 2y$$
, $v = x + y + z$, $w = x - 2y + 3z$ then find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. (07 Marks)

5 a. Obtain the reduction formula for $\int \cos^n x dx$ where n is a positive integer. (06 Marks)

b. Evaluate
$$\int_{0}^{1} x^6 \sqrt{1-x^2} dx$$
. (07 Marks)

c. Evaluate
$$\int_{0}^{1} \int_{x}^{\sqrt{x}} (x^2 + y^2) \, dy dx.$$
 (07 Marks)

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6 a. Evaluate $\int_{0}^{1} \int_{0}^{2} x^2 yz \, dz dy dx$.

(06 Marks)

b. Prove that $\sqrt{\frac{1}{2}} = \sqrt{\pi}$.

(07 Marks)

c. Show that $\int_{0}^{\pi/2} \sqrt{\sin\theta} \ d\theta \ x \ \int_{0}^{\pi/2} \frac{d\theta}{\sqrt{\sin\theta}} = \pi.$

(07 Marks)

7 a. Solve $(e^y + 1)$ Cosxdx + e^y Sinx dy = 0.

(06 Marks)

b. Solve $ydx - xdy = \sqrt{x^2 + y^2} dx$.

(07 Marks)

c. Solve $x \frac{dy}{dx} + y = x^3 y^6$.

(07 Marks)

8 a. Solve $4\frac{d^3y}{dx^3} + 4\frac{d^2y}{dx^2} + \frac{dy}{dx} = 0$.

(06 Marks)

b. Solve $\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + 3x = Sint + e^{-t}.$

(07 Marks)

c. Solve $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = xe^x \sin x$.

(07 Marks)